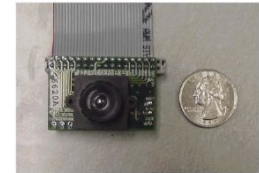


Cameras, Images and Image Processing

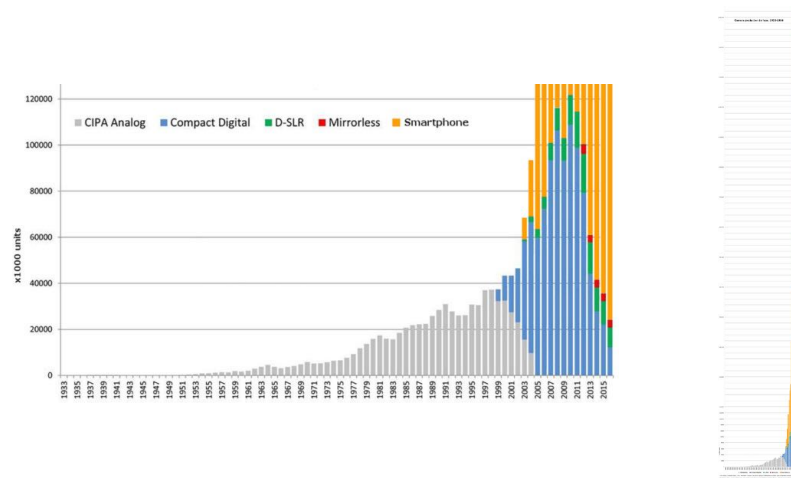
(c) Henrik I Christensen

Cameras

- Most flexible sensory modality
- Complex sensory processing
- Not discussed in any detail
- Offers wide range
- Diverse tasking of sensor
- Relatively inexpensive
- Computationally demanding



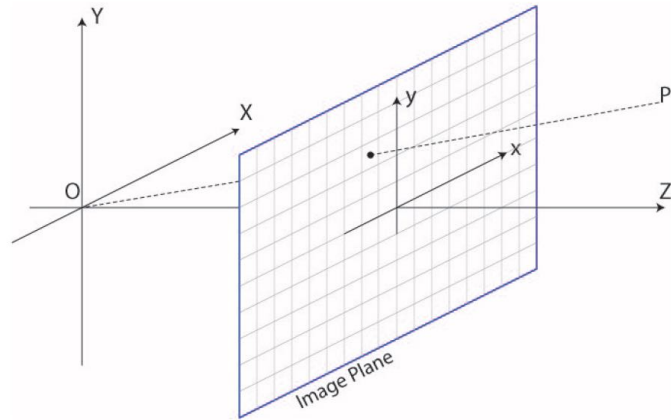
Cameras



The processing chain



The pinhole camera model



The Pin-Hole Model

- The relations are then:

$$\begin{aligned} \frac{x}{\lambda} &= \frac{X}{Z} \\ \frac{y}{\lambda} &= \frac{Y}{Z} \\ &\Rightarrow \\ x &= \frac{\lambda X}{Z} \\ y &= \frac{\lambda Y}{Z} \end{aligned}$$

In homogenous coordinates

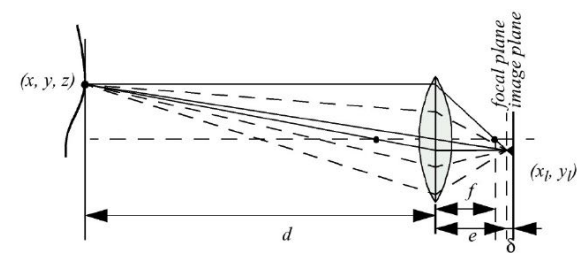
- Remember Homogeneous Coordinates?

$$\vec{p} = \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

- Define the Perspective transform as

$$\mathbf{T} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & \frac{1}{\lambda} & 0 \end{bmatrix}$$

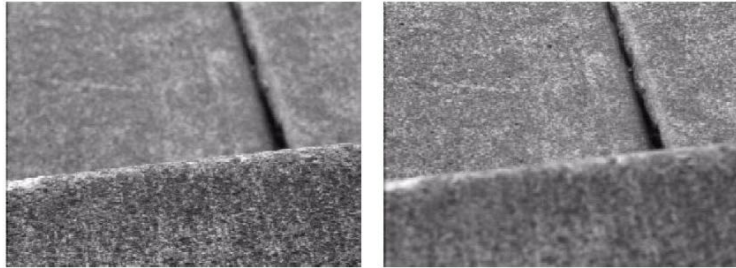
Depth from defocus



- Basic geometry: $\frac{1}{f} = \frac{1}{d} + \frac{1}{e}$
- The smear is proportional to distance

$$R = \frac{L\delta}{2e}$$

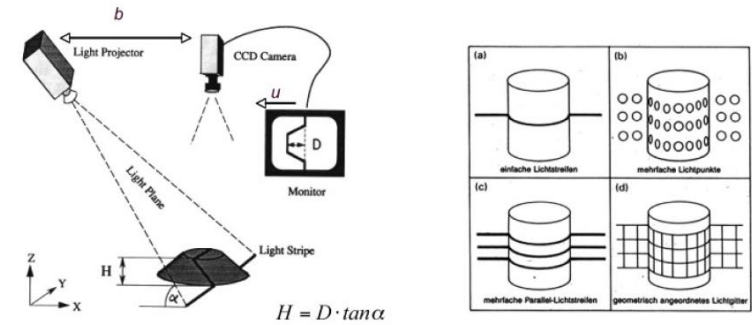
Defocus example



- Local sharpness: $LS = \sum_{x,y} |I(x,y) - I(x-1,y)|$

Structured light

- Segmentation of images is a “hard” problem
- Active illumination simplifies the problem
- In particular in industrial inspection



Images

- Images are basically a 2D array of intensity/color values
- Image types



Color



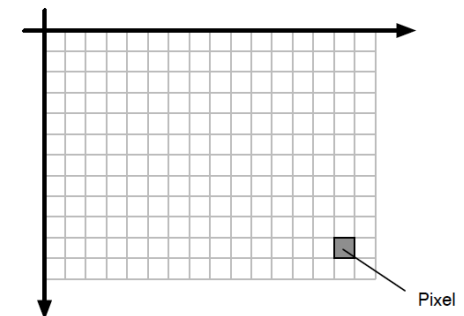
Grayscale



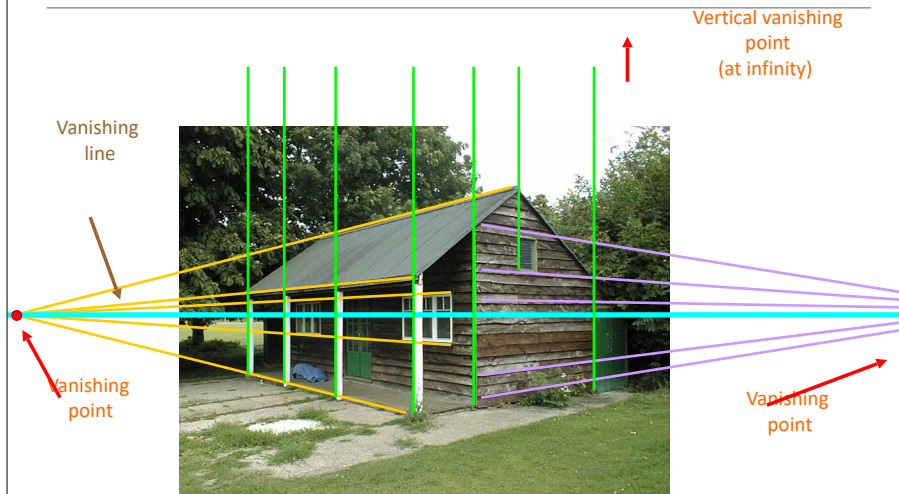
B-W

Images

- Matrix of values
- The picture element is named a **pixel**



Photographs are Projections



Slide Courtesy Antonio Criminisi

Intrinsic Calibration

3×3 Calibration Matrix K

$$m = \begin{bmatrix} u \\ v \\ w \end{bmatrix} = K \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} M = \begin{bmatrix} \alpha & s & u_0 \\ \beta & v_0 & \\ & & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ T \end{bmatrix}$$

Recover image (Euclidean) coordinates by normalizing:

$$\hat{u} = \frac{u}{w} = \frac{\alpha X + sY + u_0}{Z}$$

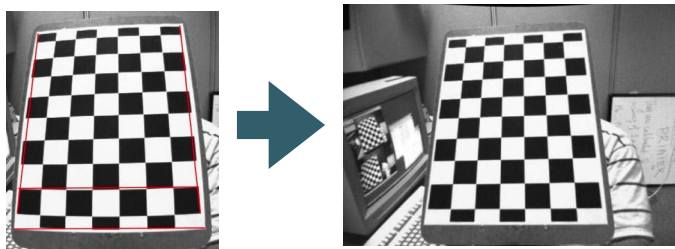
$$\hat{v} = \frac{v}{w} = \frac{\beta Y + v_0}{Z}$$

5 Degrees of Freedom !

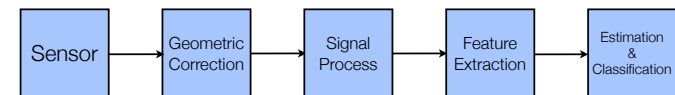
skew

Camera Calibration

- You have serious distortion on the RB5
- OpenCV (opencv-python) has tools for calibration
- https://opencv-python-tutroals.readthedocs.io/en/latest/py_tutorials/py_calib3d/py_calibration/py_calibration.html



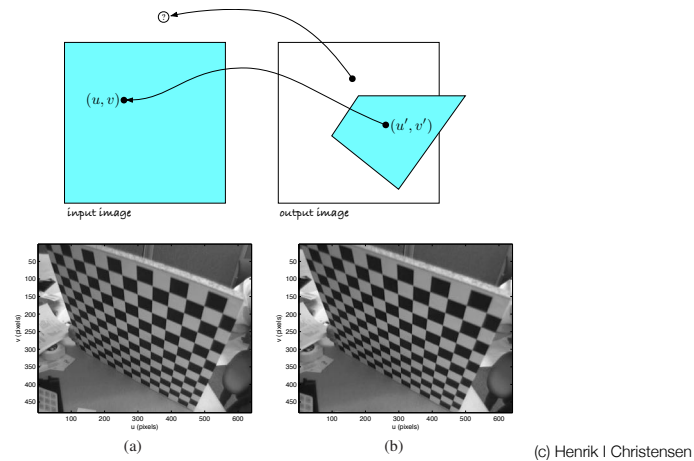
The Basic Process



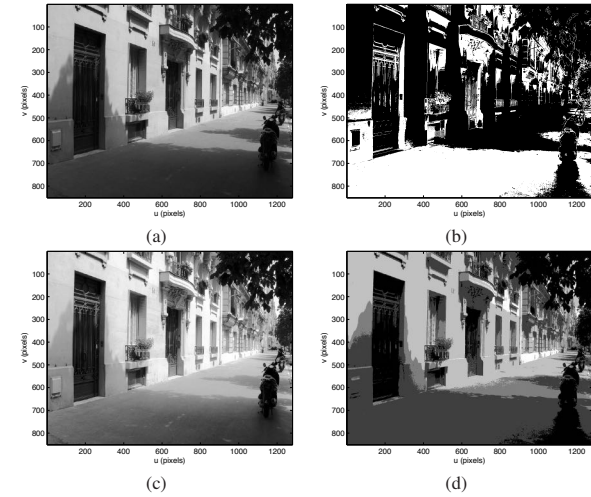
- Geometric Correction - Alignment to a calibration model
- Signal Processing - Clean up of data and signal conditioning
- Feature Extraction - Data compression and signal separation
- Estimation - Model, Space and Time Integration for estimation of key parameters
- Classification/Categorization - Assignment of one of N classes to data

Geometric Correction

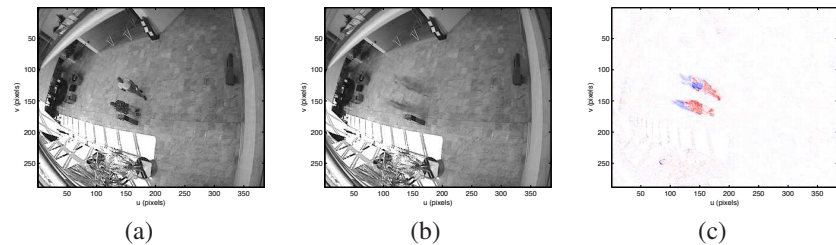
- Typically warping of signal to remove distortions



Signal enhancement



Spatial operations

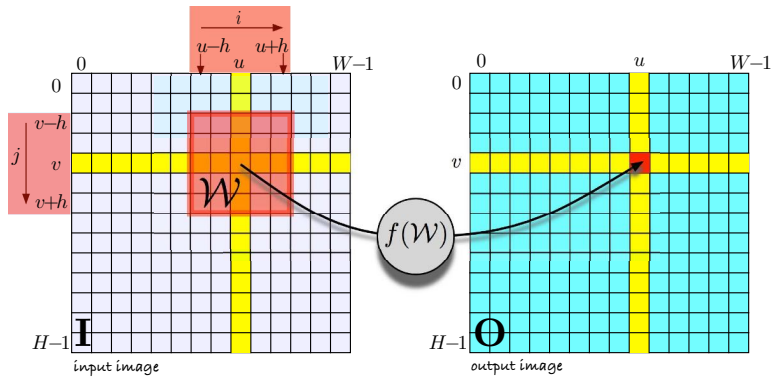


Filtering

- Noise removal
- Edge detection
- Texture description
- Multi-scale algorithms
- Feature detection
- Matched filters



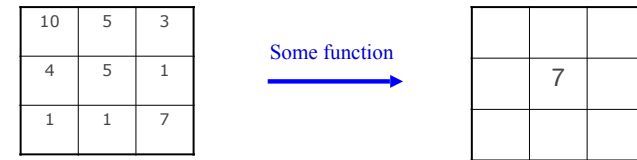
Spatial convolutions



(c) Henrik I Christensen

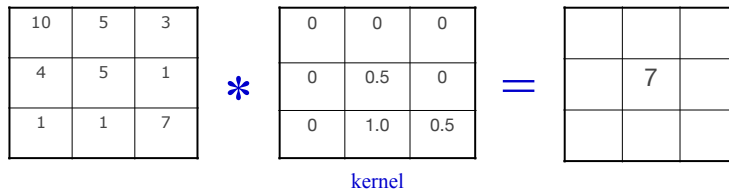
What is Image Filtering?

Modify the pixels in an image based on some function of a local neighborhood of the pixels

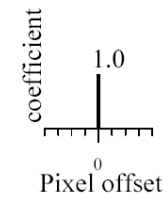


Linear Filtering

- Linear case is simplest and most useful
 - Replace each pixel with a linear combination of its neighbors.
- Prescription for linear combination is called the **convolution kernel**.

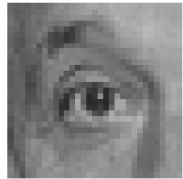


Filtering Examples

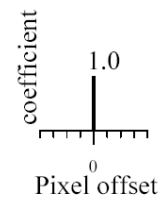


?

Filtering Examples: Identity



original

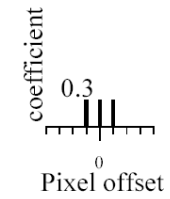


Filtered
(no change)

Filtering Examples



original

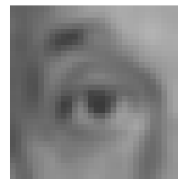
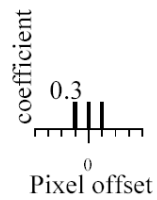


?

Filtering Examples: Blur



original

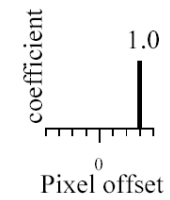


Blurred (filter
applied in both
dimensions).

Filtering Examples

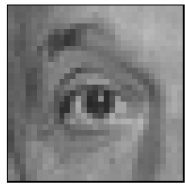


original

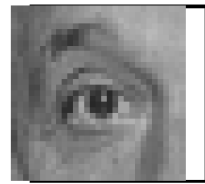
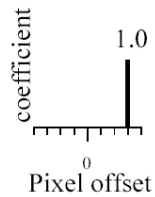


?

Filtering Examples: Shift



original



shifted

Convolutions to enhance images

Properties of convolution. Convolution obeys the familiar rules of algebra, it is commutative

$$A \otimes B = B \otimes A$$

associative

$$A \otimes B \otimes C = (A \otimes B) \otimes C = A \otimes (B \otimes C)$$

distributive (superposition applies)

$$A \otimes (B + C) = A \otimes B + A \otimes C$$

linear

$$A \otimes (\alpha B) = \alpha(A \otimes B)$$

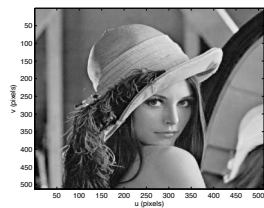
and shift invariant — if $S(\cdot)$ is a spatial shift then

$$A \otimes S(B) = S(A \otimes B)$$

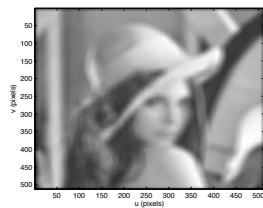
that is, convolution with a shifted image is the same as shifting the result of the convolution with the unshifted image.

(c) Henrik I Christensen

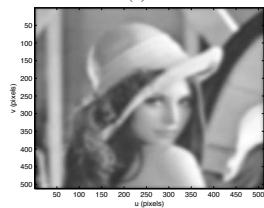
Smoothing Example



(a)



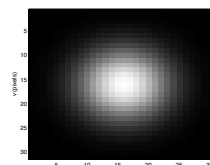
(b)



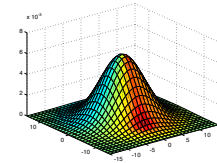
(c)

(c) Henrik I Christensen

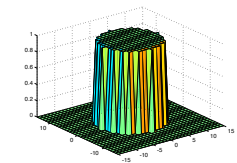
A few typical kernels



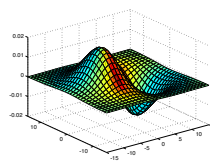
(a) Gaussian as image



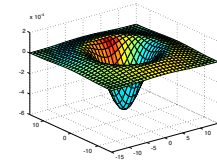
(b) Gaussian



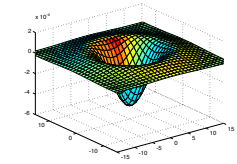
(c) Top hat ($r = 8$)



(d) Derivative of Gaussian



(e) Laplacian of Gaussian



(f) Difference of Gaussian

(c) Henrik I Christensen

Convolution

- Represent these weights as an image, H
- H is usually called the **kernel**
- Operation is called **convolution**

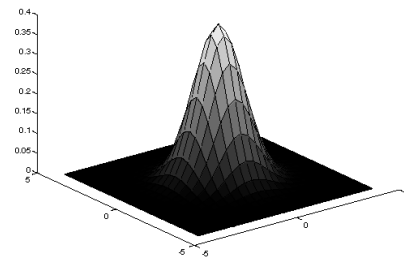
$$R_{ij} = \sum_{u,v} H_{i-u,j-v} F_{uv}$$

Example: Smoothing by Averaging



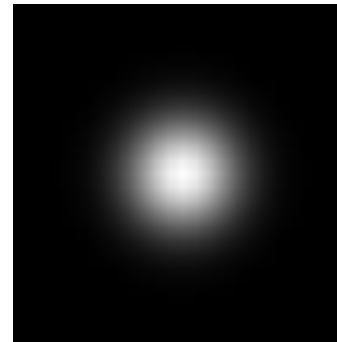
Smoothing with a Gaussian

- Averaging does not model defocussed lens well
- impulse response should be fuzzy blob



An Isotropic Gaussian

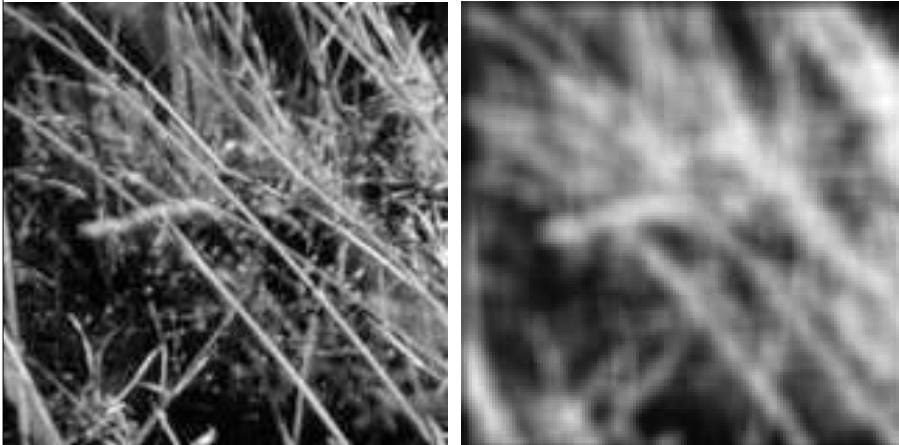
- The picture shows a smoothing kernel proportional to



$$\exp\left(-\left(\frac{x^2 + y^2}{2\sigma^2}\right)\right)$$

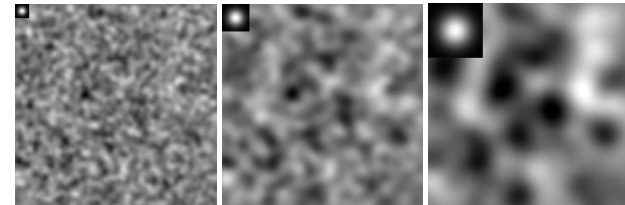
- reasonable model of a circularly symmetric blob

Smoothing with a Gaussian



Filter responses are correlated

- Correlated over scales similar to scale of filter
- Filtered noise is sometimes useful
 - looks like some natural textures, can be used to simulate fire, etc.



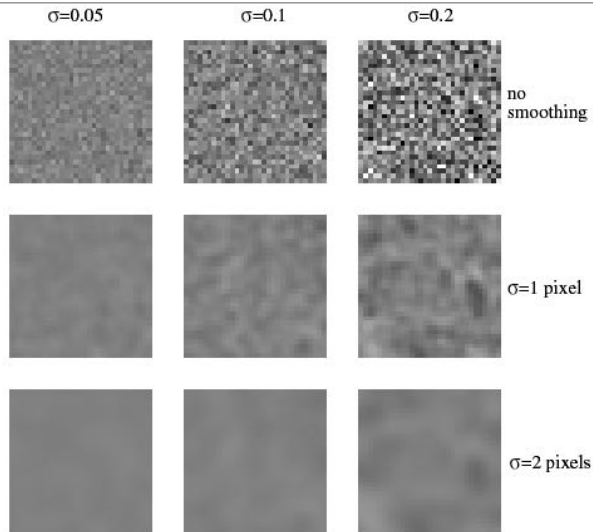
sigma=1



sigma=16



The effects of smoothing

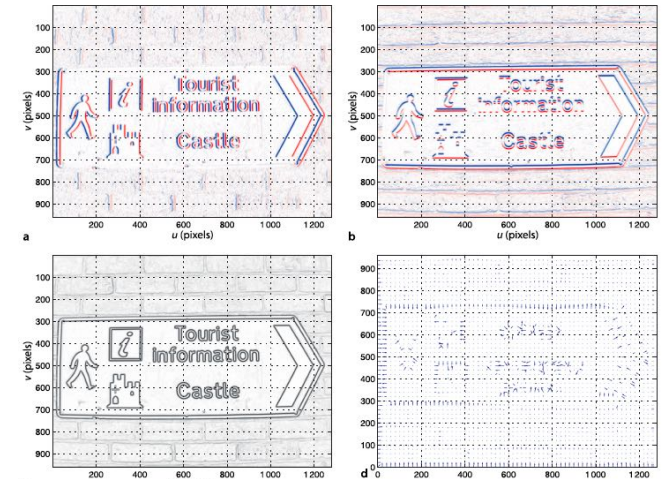


Edge Detection

☐ Sobel Kernel (Corke Chapter 12)

```
>> Du = ksobel
Du =
    -1    0    1
     -2    0    2
     -1    0    1
```

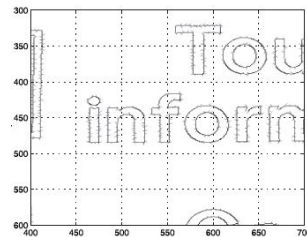
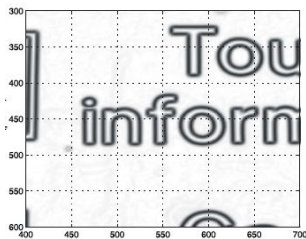
Magnitude
& direction



|DoG| vs. Canny

☐ Canny: smart post-processing of edge

☐ Derivative of Gaussian operator, then take magnitude



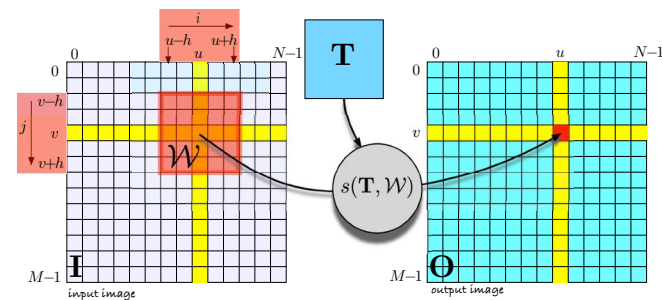
$$\nabla I = \mathbf{D} \otimes (\mathbf{G}(\sigma) \otimes I) = \underbrace{(\mathbf{D} \otimes \mathbf{G}(\sigma))}_{\text{DoG}} \otimes I$$

$$G_u(u, v) = -\frac{u}{2\pi\sigma^2} e^{-\frac{u^2+v^2}{2\sigma^2}}$$

```
>> Iu = iconv( castle, -kdgauiss(2) );
>> Iv = iconv( castle, -kdgauiss(2)' );
>> m = sqrt( Iu.^2 + Iv.^2 );
```

Template matching

- In some cases it is entirely possible to match signals to templates
- The template could be sub-images, or processed versions of an arbitrary signal



Typical performance metrics

Sum of absolute differences

$$\text{SAD} \quad s = \sum_{(u,v) \in \mathbf{I}} |I_1[u,v] - I_2[u,v]| \quad \text{sad}$$

$$\text{ZSAD} \quad s = \sum_{(u,v) \in \mathbf{I}} |(I_1[u,v] - \bar{I}_1) - (I_2[u,v] - \bar{I}_2)| \quad \text{zsad}$$

Sum of squared differences

$$\text{SSD} \quad s = \sum_{(u,v) \in \mathbf{I}} (I_1[u,v] - I_2[u,v])^2 \quad \text{ssd}$$

$$\text{ZSSD} \quad s = \sum_{(u,v) \in \mathbf{I}} ((I_1[u,v] - \bar{I}_1) - (I_2[u,v] - \bar{I}_2))^2 \quad \text{zssd}$$

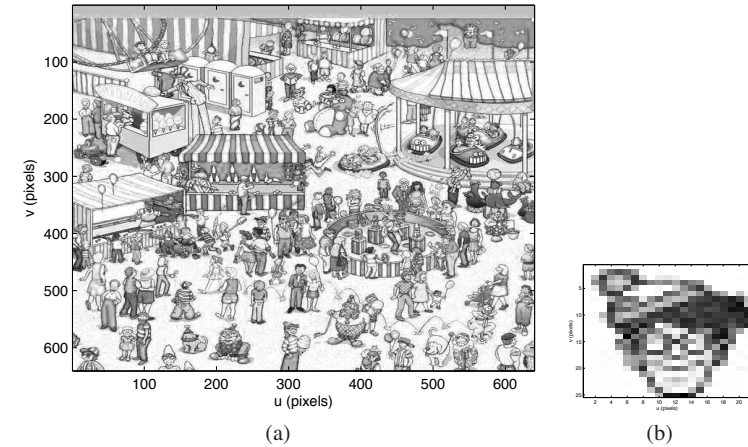
Cross correlation

$$\text{NCC} \quad s = \frac{\sum_{(u,v) \in \mathbf{I}} I_1[u,v] \cdot I_2[u,v]}{\sqrt{\sum_{(u,v) \in \mathbf{I}} I_1^2[u,v] \cdot \sum_{(u,v) \in \mathbf{I}} I_2^2[u,v]}} \quad \text{ncc}$$

$$\text{ZNCC} \quad s = \frac{\sum_{(u,v) \in \mathbf{I}} (I_1[u,v] - \bar{I}_1) \cdot (I_2[u,v] - \bar{I}_2)}{\sqrt{\sum_{(u,v) \in \mathbf{I}} (I_1[u,v] - \bar{I}_1)^2 \cdot \sum_{(u,v) \in \mathbf{I}} (I_2[u,v] - \bar{I}_2)^2}} \quad \text{zncc}$$

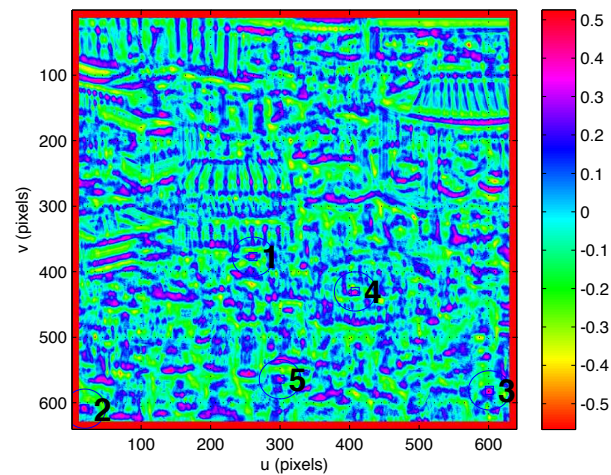
(c) Henrik I Christensen

Where is waldo?



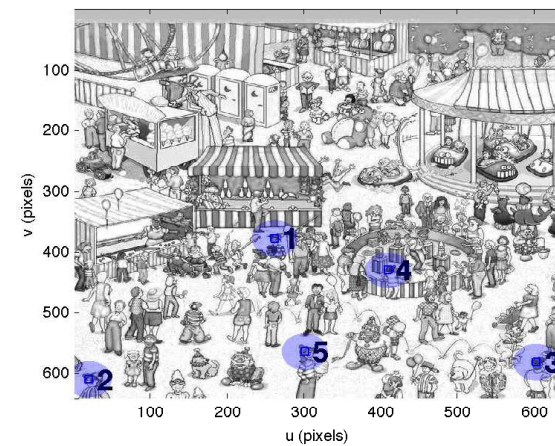
(c) Henrik I Christensen

Where is Waldo?



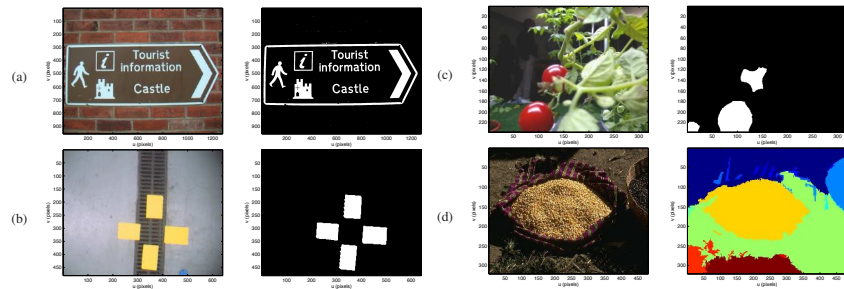
(c) Henrik I Christensen

Where is Waldo?



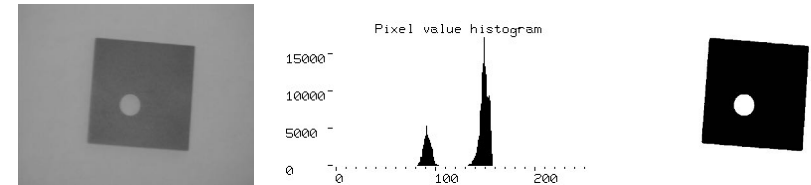
(c) Henrik I Christensen

Feature Extraction



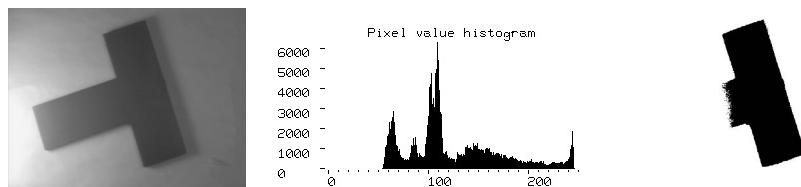
(c) Henrik I Christensen

Simple object detection



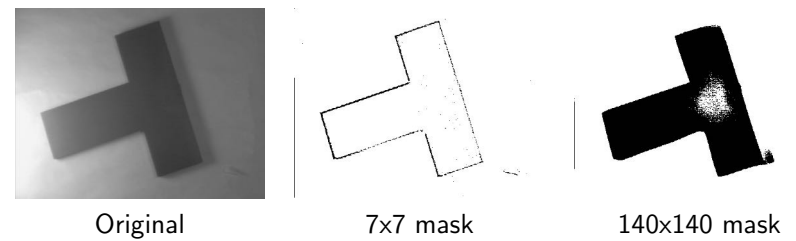
(c) Henrik I Christensen

If only life was that simple



(c) Henrik I Christensen

Adaptive thresholding



(c) Henrik I Christensen

Feature extraction

- Broad set of possible features depending on sensor modality
 - Point Estimation
 - Line Estimation (mathematical vs finite lines)
 - Place Estimation
 - Geometric features (#holes, shape descriptors)
 - Statistical Features (typical moments, central moments, ...)
 - Basic geometry

(c) Henrik I Christensen

Line Estimation

- Lines are a predominant feature in engineered environments
- There is an abundance of methods for line estimation
- LSQ, Split-Merge, Hough, EM-estimation,
- RANSAC is frequently used (Fischler & Bolles, 1981)

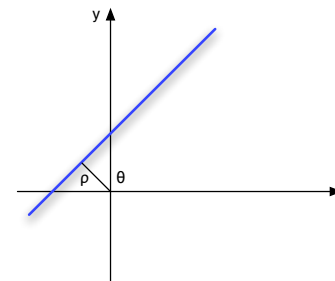
(c) Henrik I Christensen

Voting based methods

- Voting provides a simple estimator for detection
- Voting requires:
 - 1 A Voting Space
 - 2 A voting function (structure function)
 - 3 A decision function (often local extrema)
- Hough (1962) is one of the most widely used. Can also be used for lines and other shapes (Ballard, 1981)

(c) Henrik I Christensen

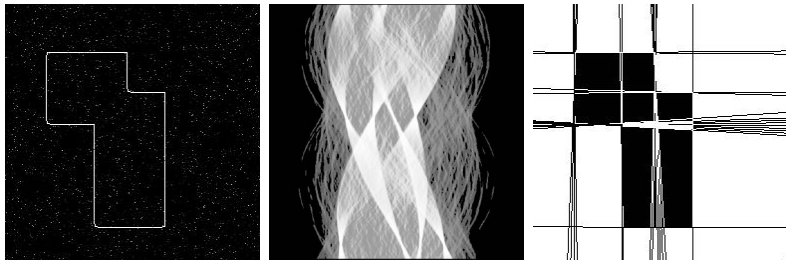
Hough based estimator



- Line model:
$$\rho = x * \cos(\theta) + y * \sin(\theta)$$
- Voting space: $[\theta, \rho]$
- Voter: traverse θ space
- Local maximum w. NMS
- for all points in (x,y)
for each $\theta : 0 \rightarrow \pi$
calc ρ and increment (θ, ρ)
- Generates infinite lines.

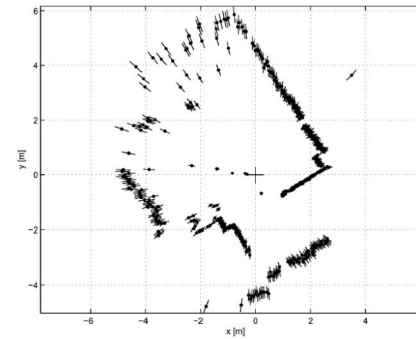
(c) Henrik I Christensen

Basic Hough Example



(c) Henrik I Christensen

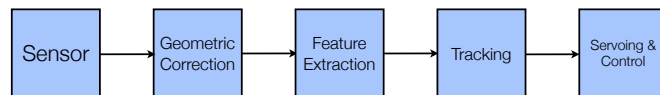
Hough on polar / range - bearing data



- Scanning is in polar coordinates.
- The density of points is varying.
- Close structure will accumulate more points.
- Range weighting can compensate. Proposed by Forsberg *et al.* (1993).
Weight by $\frac{1}{\cos(\psi_i - \theta)}$

(c) Henrik I Christensen

The approach for visual navigation



- Need to detect robust features for objects (we will discuss more next two sessions)
- Tracking of features over time to “keep” features in view
- Control vehicle to achieve the task objective

(c) Henrik I Christensen

RANSAC - Random Sampling Consensus

- Estimation of parameters from N data items
- There are M data point in total
- How do we find the best parameters when there are many outliers?



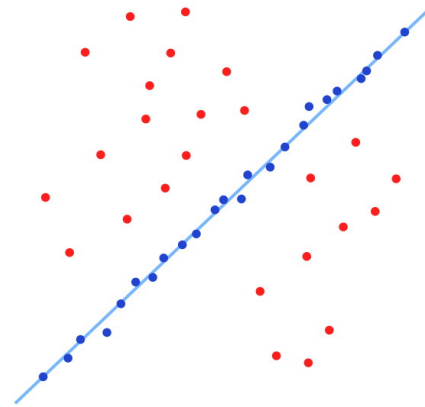
(c) Henrik I Christensen

RANSAC - Algorithm

- 1 selects N data items at random
- 2 estimates parameter \vec{x}
- 3 finds how many data items (of M) fit the model with parameter vector \vec{x} within a user given tolerance. Call this K.
- 4 if K is big enough, accept fit and exit with success.
- 5 repeat 1..4 L times
- 6 fail if you get here

(c) Henrik I Christensen

RANSAC Example Result



(c) Henrik I Christensen

LSQ line fitting

- Least square minimization:

- Line equation: $y = ax + b$
- Error in fit: $\sum_i (y_i - ax_i - b)^2$
- Solution:

$$\begin{pmatrix} \bar{y}^2 \\ \bar{y} \end{pmatrix} = \begin{pmatrix} \bar{x}^2 & \bar{x} \\ \bar{x} & 1 \end{pmatrix} \begin{pmatrix} a \\ b \end{pmatrix}$$

- Minimizes vertical errors. Non-robust!

(c) Henrik I Christensen

TLS line fitting

- Line equation: $ax + by + c = 0$
- Error in fit: $\sum_i (ax_i + by_i + c)^2$ where $a^2 + b^2 = 1$.
- Solution:

$$\begin{pmatrix} \bar{x}^2 - \bar{x}\bar{x} & \bar{x}\bar{y} - \bar{x}\bar{y} \\ \bar{x}\bar{y} - \bar{x}\bar{y} & \bar{y}^2 - \bar{y}\bar{y} \end{pmatrix} \begin{pmatrix} a \\ b \end{pmatrix} = \mu \begin{pmatrix} a \\ b \end{pmatrix}$$

where μ is a scale factor.

- $c = -a\bar{x} - b\bar{y}$

(c) Henrik I Christensen

Summary

- Starting to think about images as a primary modality for feedback
- The main sensor for CSE276A homework
- There are much more to image processing than we can cover. The book (Corke, 2023) covers much more material
- Most of the processing covered by the OpenCV library - <https://opencv.org/>